

Particle Video:
Long-Range Video Motion Estimation
using Point Trajectories

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Long-Range Motion Estimation



Long-Range Motion Estimation



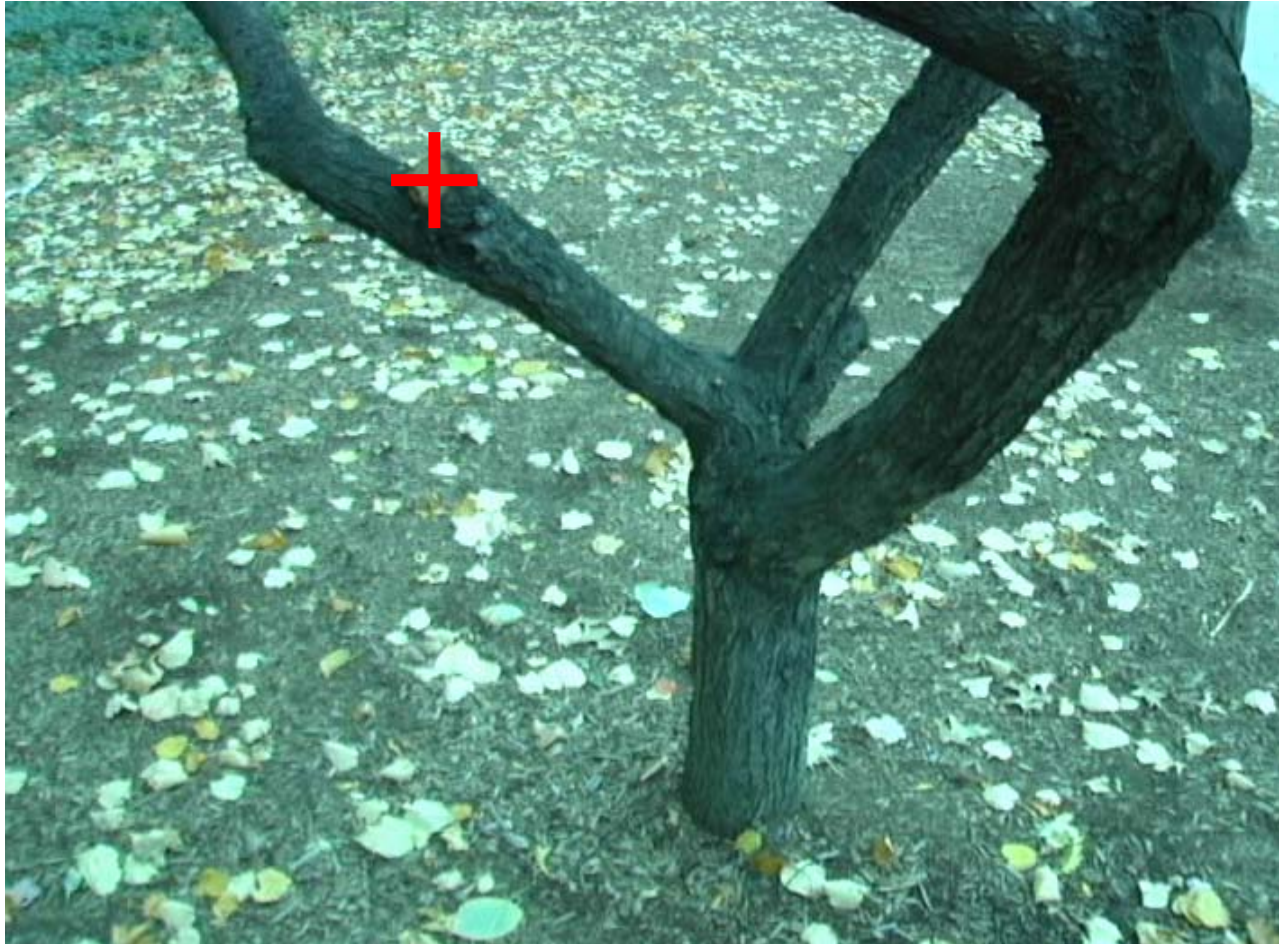
Long-Range Motion Estimation



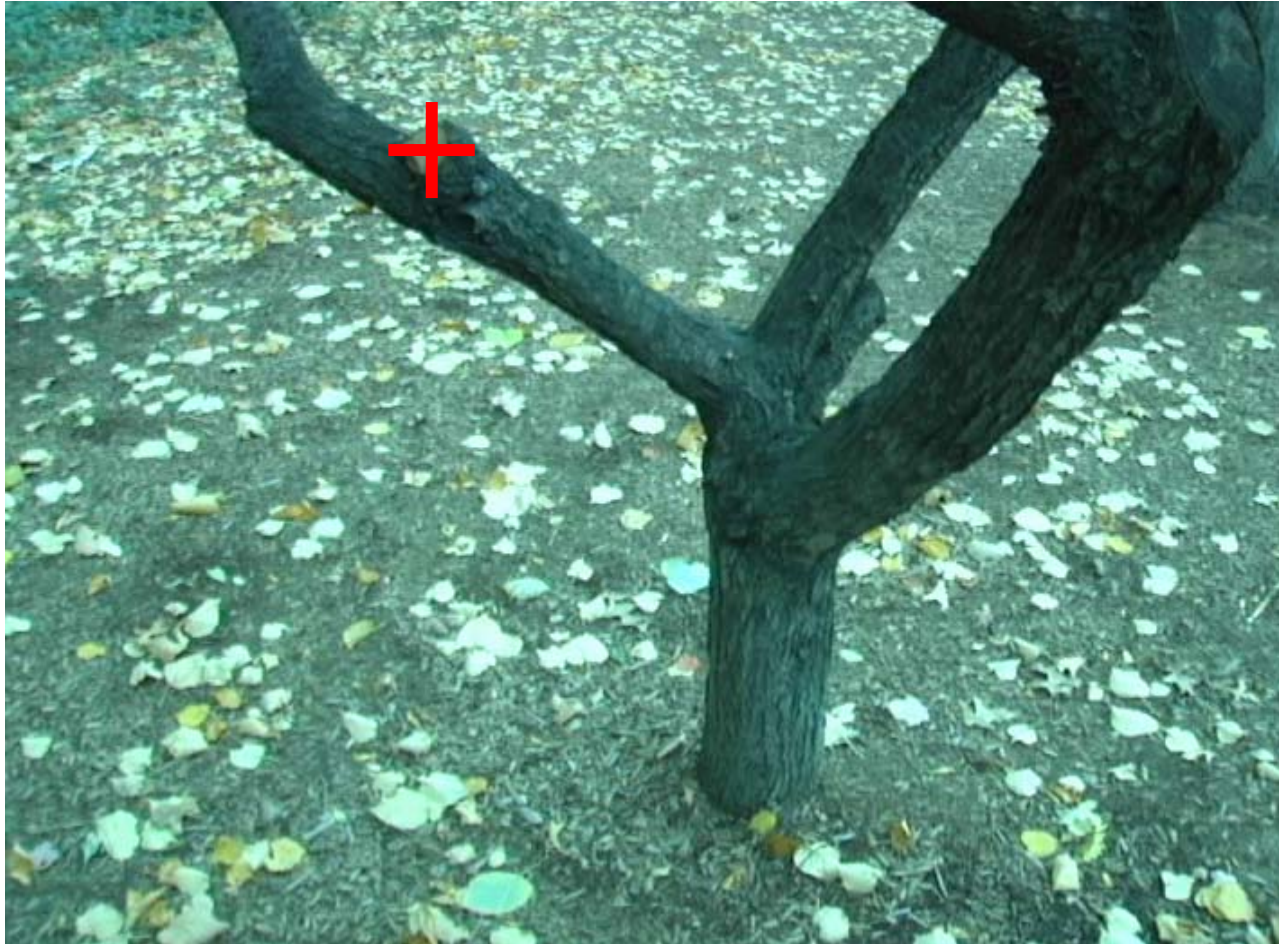
Long-Range Motion Estimation



Long-Range Motion Estimation



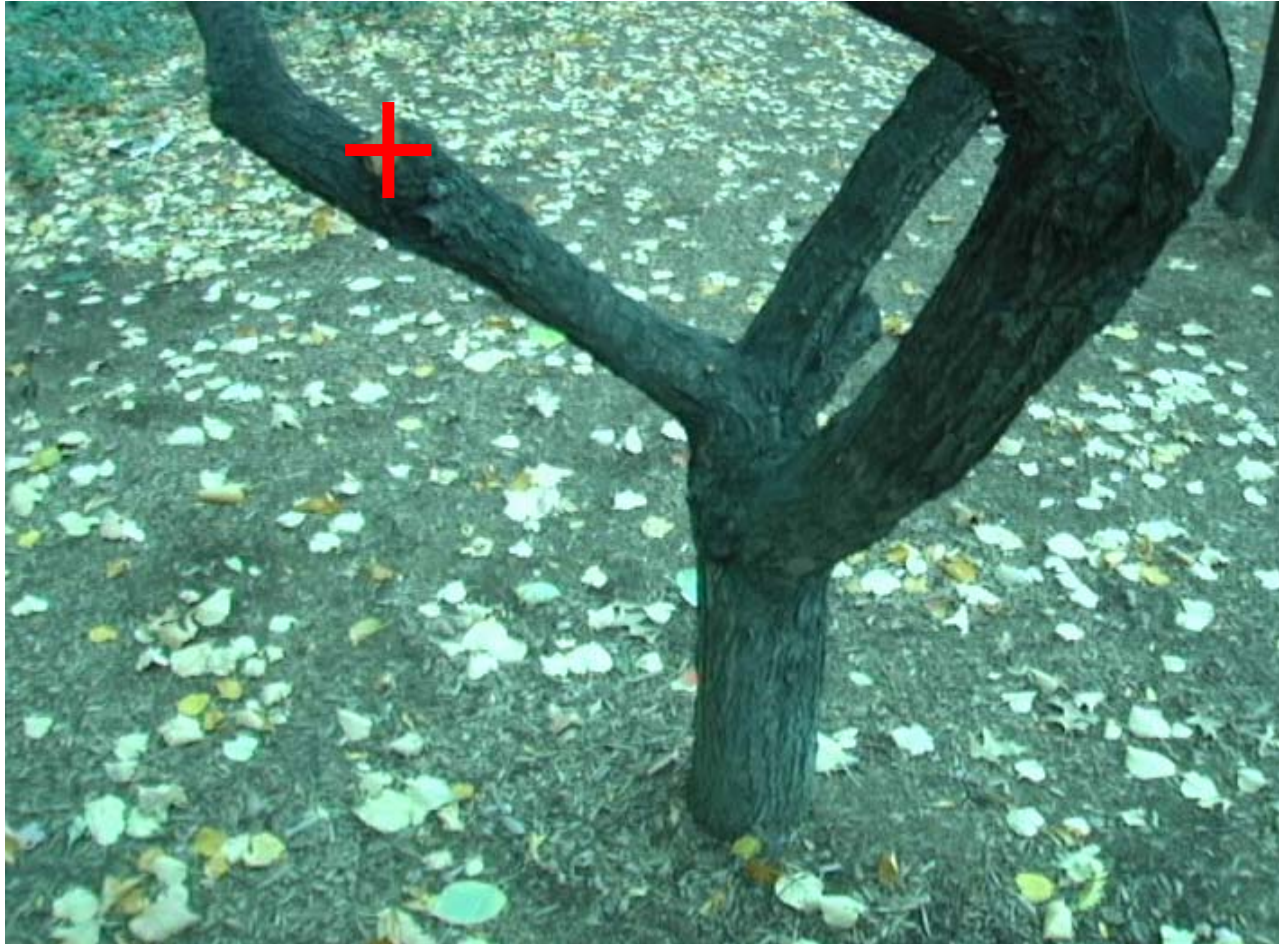
Long-Range Motion Estimation



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Long-Range Motion Estimation



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Long-Range Motion Estimation



Long-Range Motion Estimation



Long-Range Motion Estimation



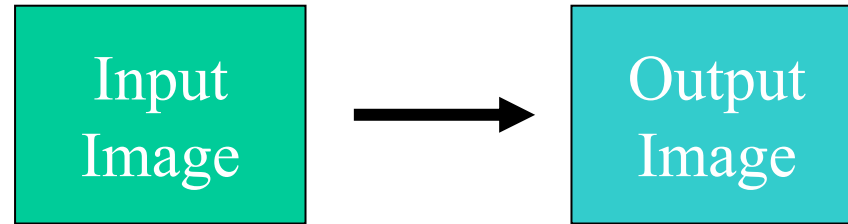
Long-Range Motion Estimation



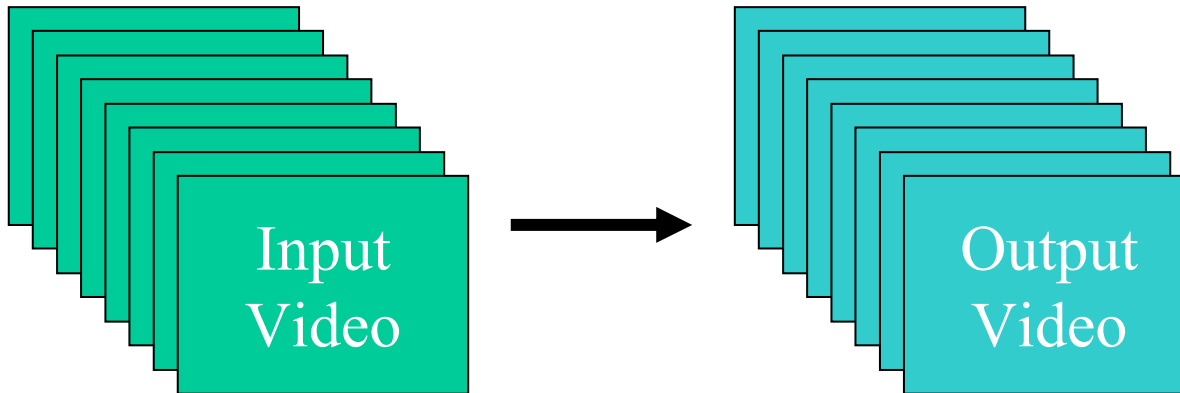
Long-Range Motion Estimation



Applications



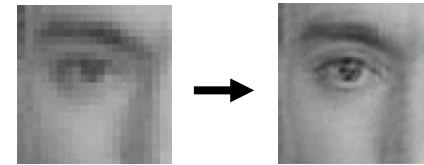
Photoshop, etc.



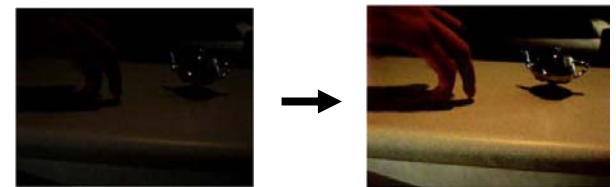
Particle-based editor

Applications

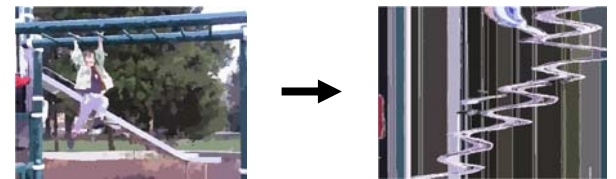
- Super-resolution
- Noise removal
- High dynamic range video
- Image filtering
- Video segmentation
- Matting / rotoscoping
- Object removal



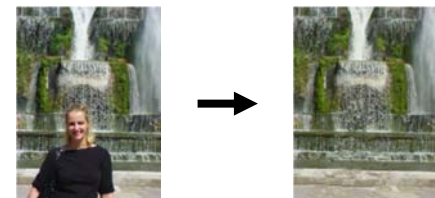
[Capel and Zisserman 2001]



[Bennett and McMillan 2005]



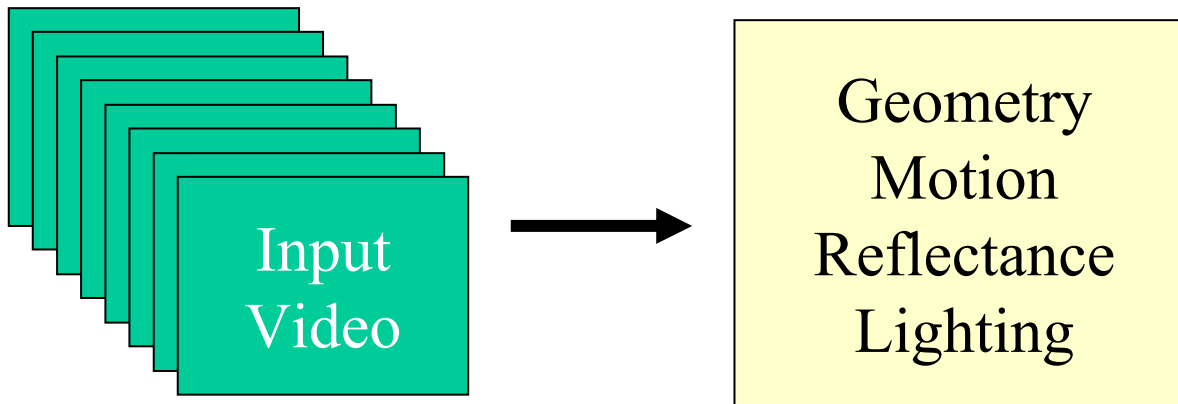
[Jue Wang *et al.* 2004]



[Criminisi *et al.* 2003]

Applications

Long-range motion estimation is a step toward a larger goal: video decomposition.



Design Goals



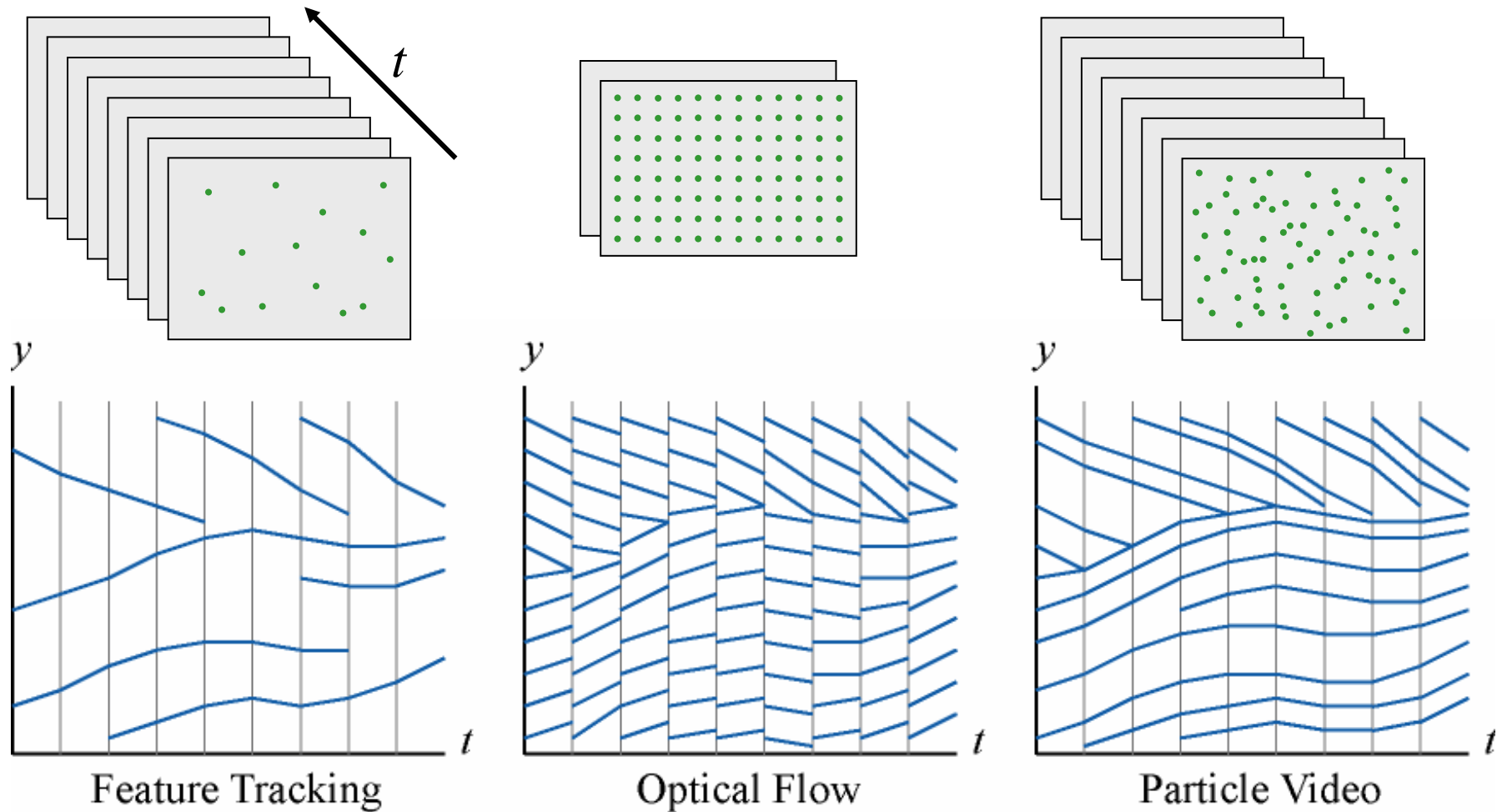
Design Goals



Design Goals



Related Work

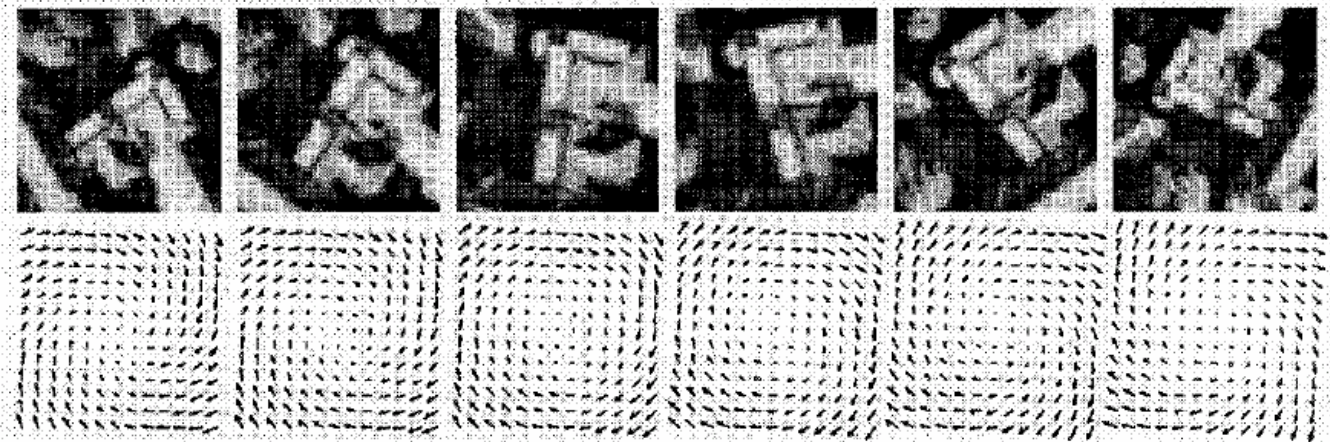


Related Work: Optical Flow

Temporal smoothness assumption

[Black and Anandan 1991, Chin *et al.* 1994,
Elad and Feuer 1998, Shi and Malik 1998]

2-st image 21-st image 41-st image 61-st image 81-st image 101-st image



[Elad and Feuer 1998]

Related Work: Optical Flow

Rank-based optical flow

[Irani 1999, Brand 2001]

$$\begin{array}{c}
 \begin{array}{c} \nearrow \\ \circlearrowleft \\ \searrow \end{array} \mathbf{R} \left(\begin{array}{c} \text{[Face 1]} \\ \mathbf{c}_1 \mathbf{S}_1 \end{array} + \begin{array}{c} \text{[Face 2]} \\ \mathbf{c}_2 \mathbf{S}_2 \end{array} + \begin{array}{c} \text{[Face 3]} \\ \mathbf{c}_3 \mathbf{S}_3 \end{array} + \begin{array}{c} \text{[Face 4]} \\ \mathbf{c}_4 \mathbf{S}_4 \end{array} \right) + \begin{array}{c} \nearrow \\ \mathbf{t} \end{array} = \begin{array}{c} \text{[Face 5]} \\ \mathbf{P} \end{array} \\
 \\
 \mathbf{M} \times \mathbf{S} \oplus \mathbf{T} = \mathbf{P}
 \end{array}$$



[Brand 2001]

Related Work: Optical Flow

Occlusion labeling:

- Pixel dissimilarity

[Silva and Santos-Victor 2001, Xiao *et al.* 2006]

- Forward / backward mismatch

[Alvarez *et al.* 2002]

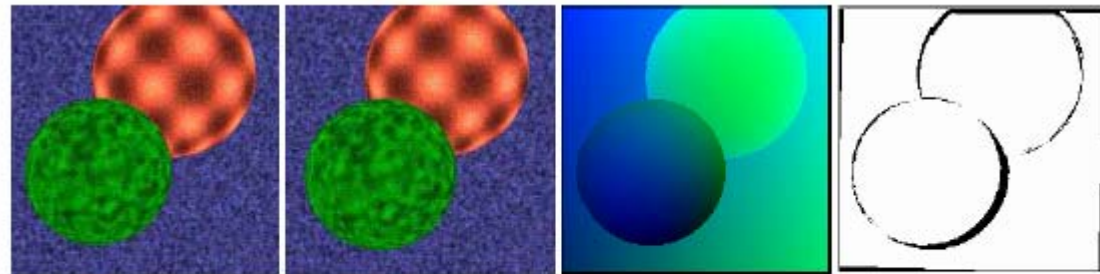


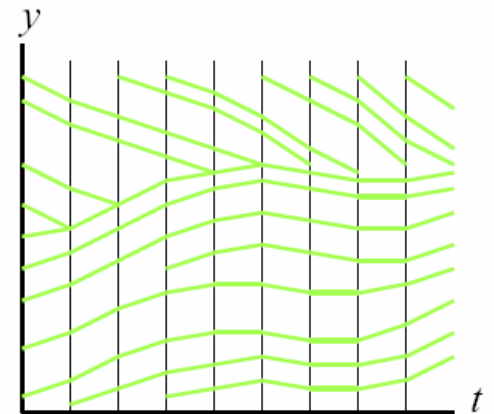
Fig. 2. One of the synthetic scenes used in the experiments. Left two images: input; middle right: ground truth optical flow; right: ground truth occlusions

[Stretcha *et al.* 2004]

Particle Approach

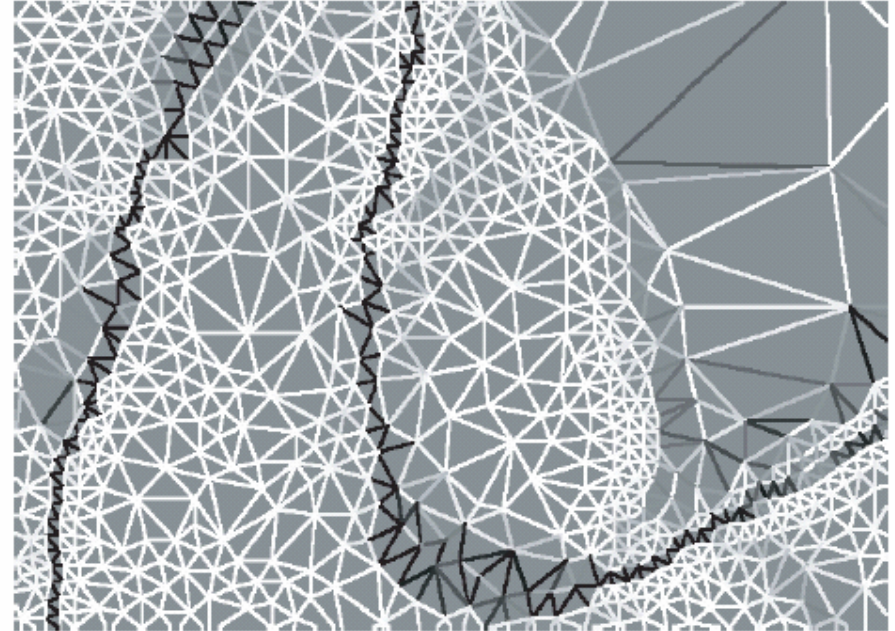


- Particles are small
- Adaptive density
- Does not assume temporal motion smoothness



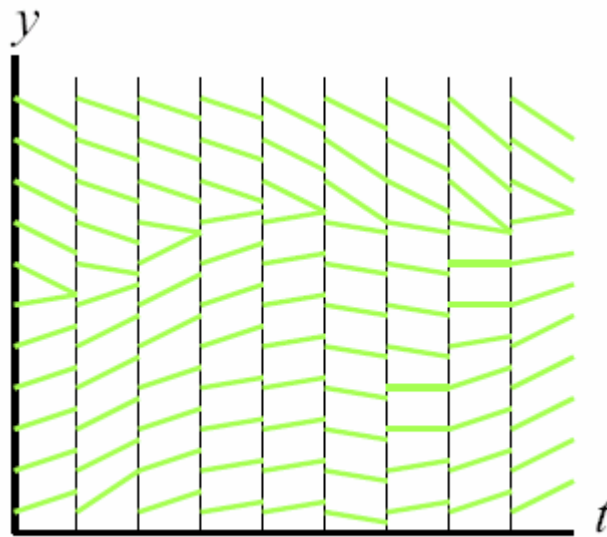
Particle Video

Particle Approach

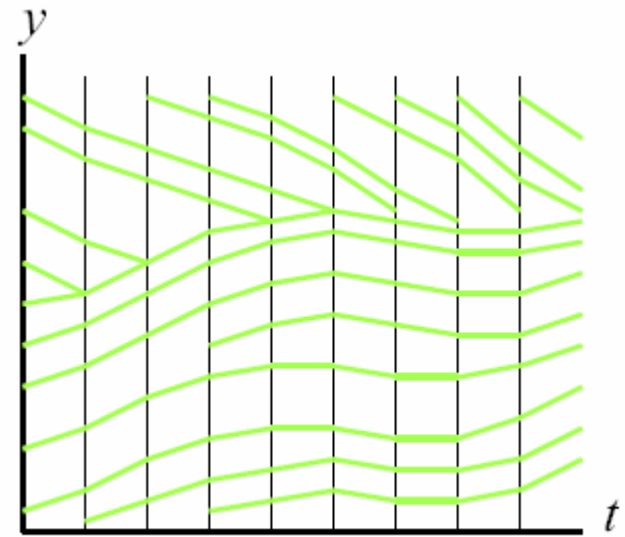


- Triangulation implicitly represents particle grouping
- Non-parametric
- Not layer-based
- No segmentation
- Not planar or rigid components

Optical Flow as Input



Optical Flow



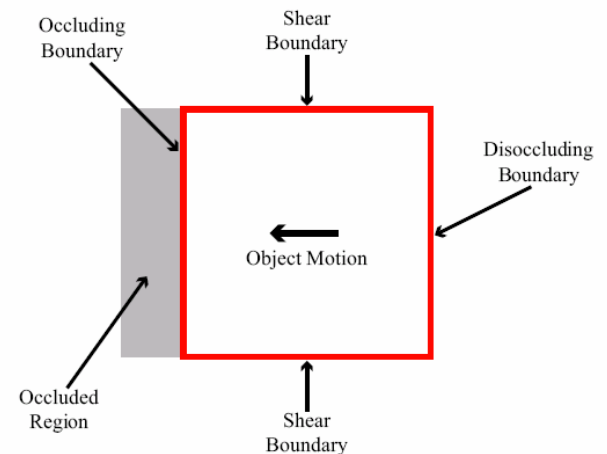
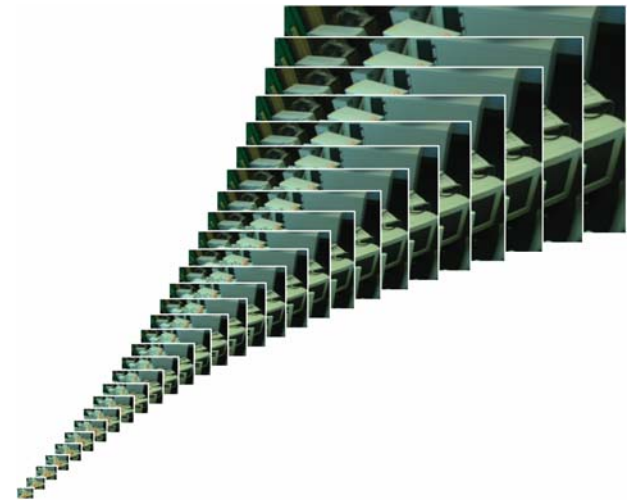
Particle Video

An Optical Flow Algorithm

At each resolution level:

- Variational flow update
 - Similar to [Brox *et al.* 2004]
- Label occluded regions
- Bilateral flow filter
 - Similar to [Xiao *et al.* 2006]

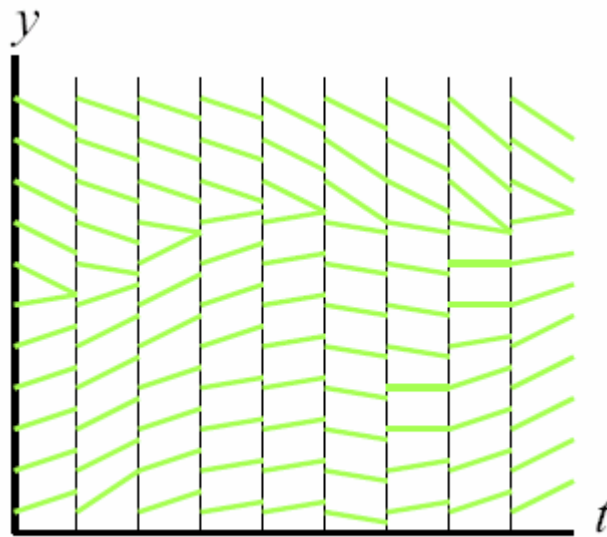
(see paper for more details)



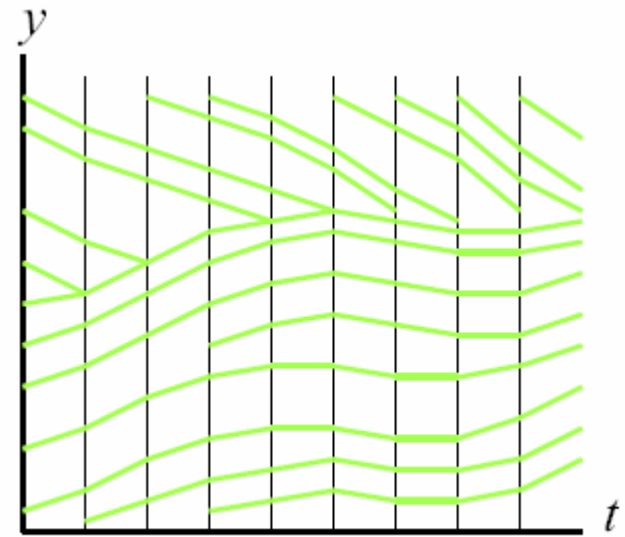
Optical Flow Results



Particle Video Algorithm

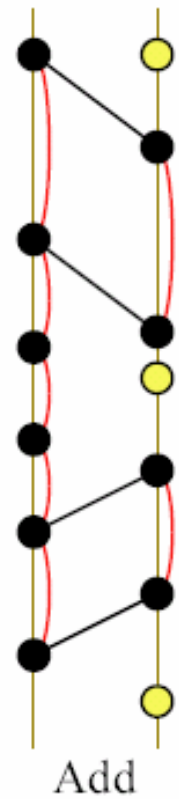
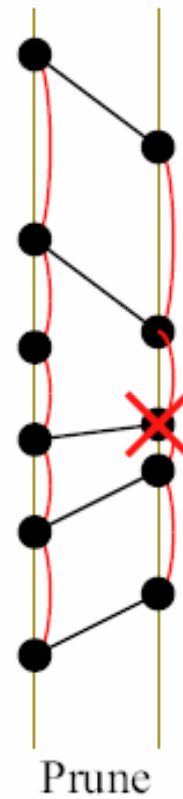
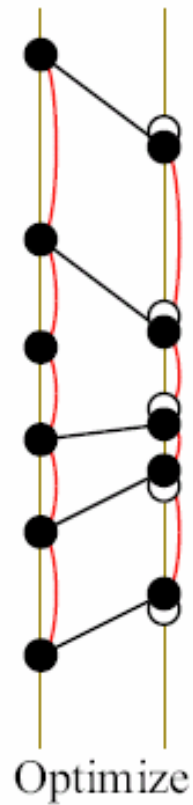
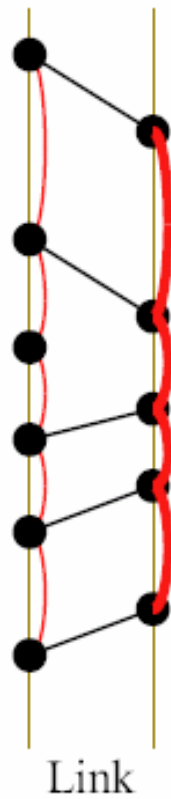
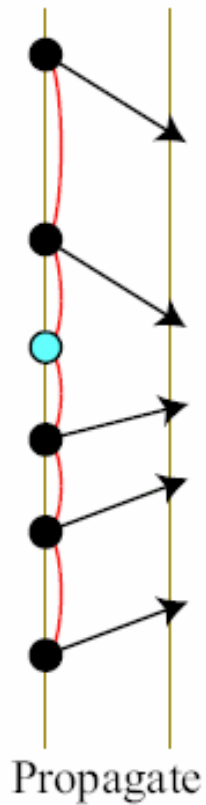


Optical Flow



Particle Video

Particle Video Steps



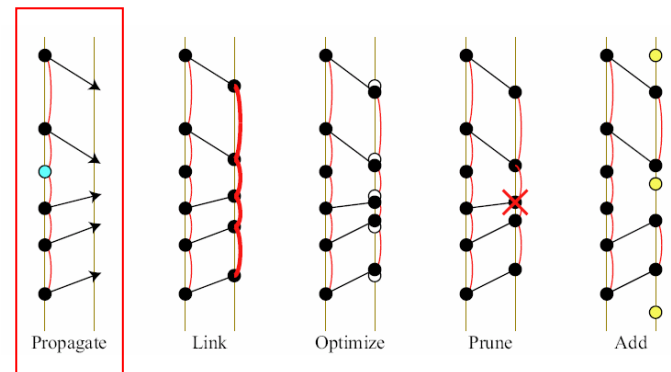
Particle Propagation

Forward propagation:

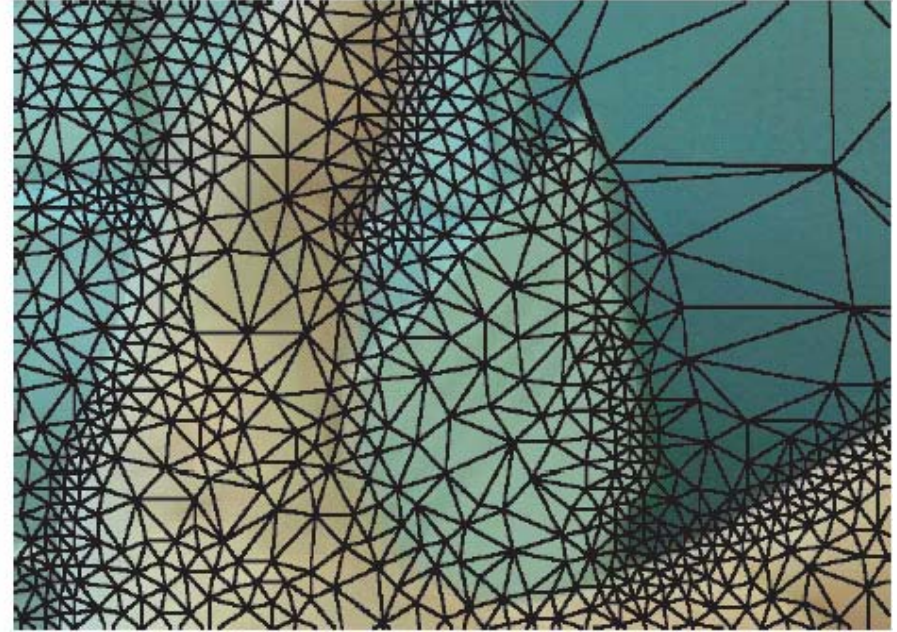
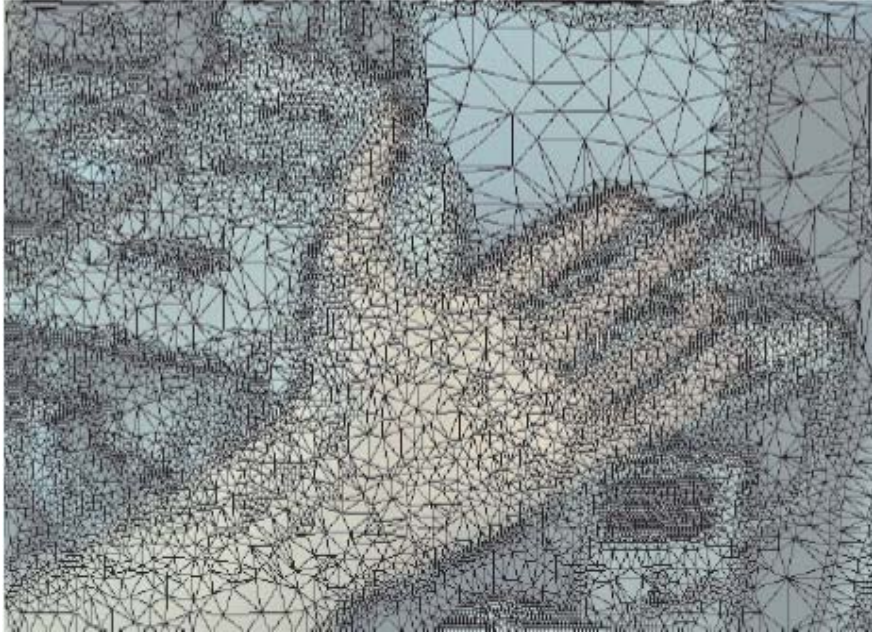
$$x_i(t) = x_i(t-1) + u(x_i(t-1), y_i(t-1), t-1),$$

$$y_i(t) = y_i(t-1) + v(x_i(t-1), y_i(t-1), t-1).$$

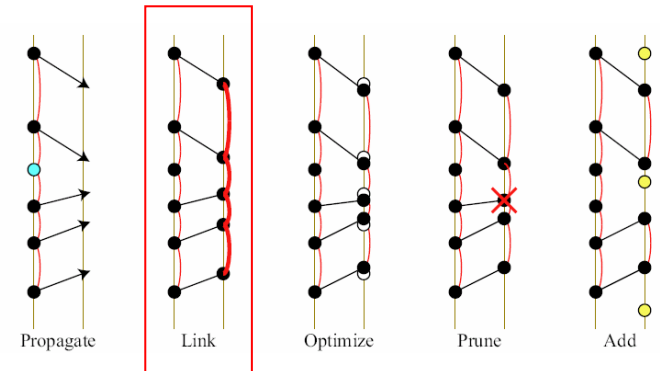
Particles in occluded regions
are not propagated.



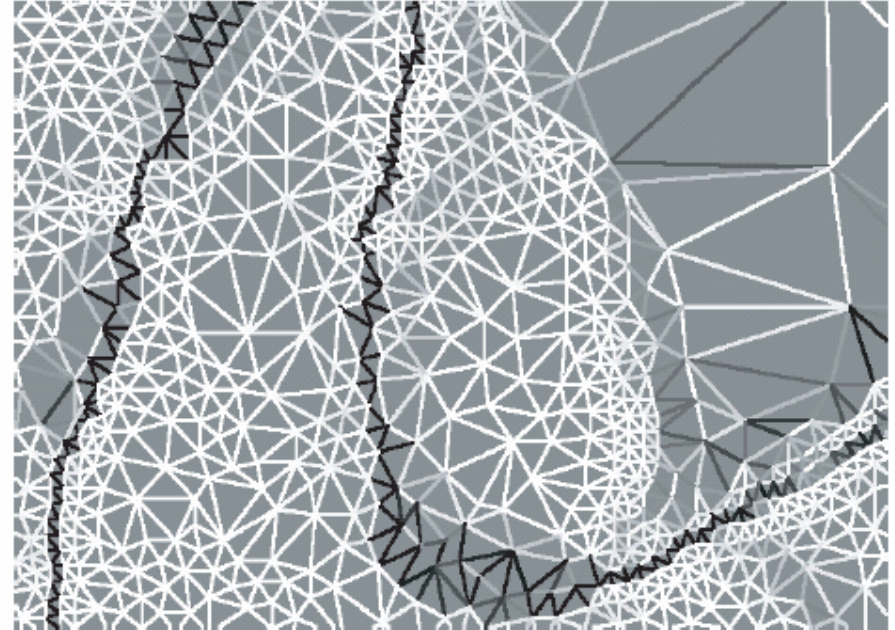
Particle Linking



- Delaunay Triangulation [Lischinski 1994]
- Create link if Delaunay edge exists in current frame or adjacent frame

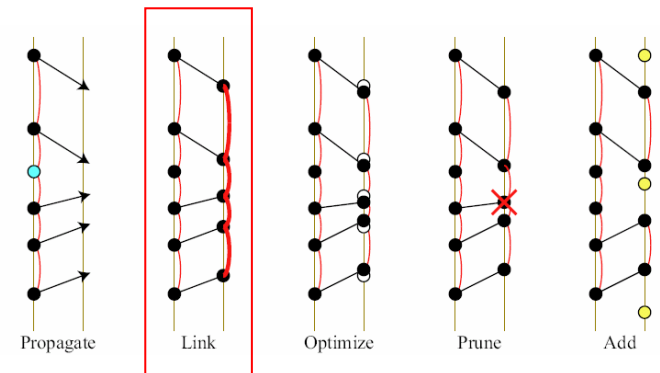


Particle Linking

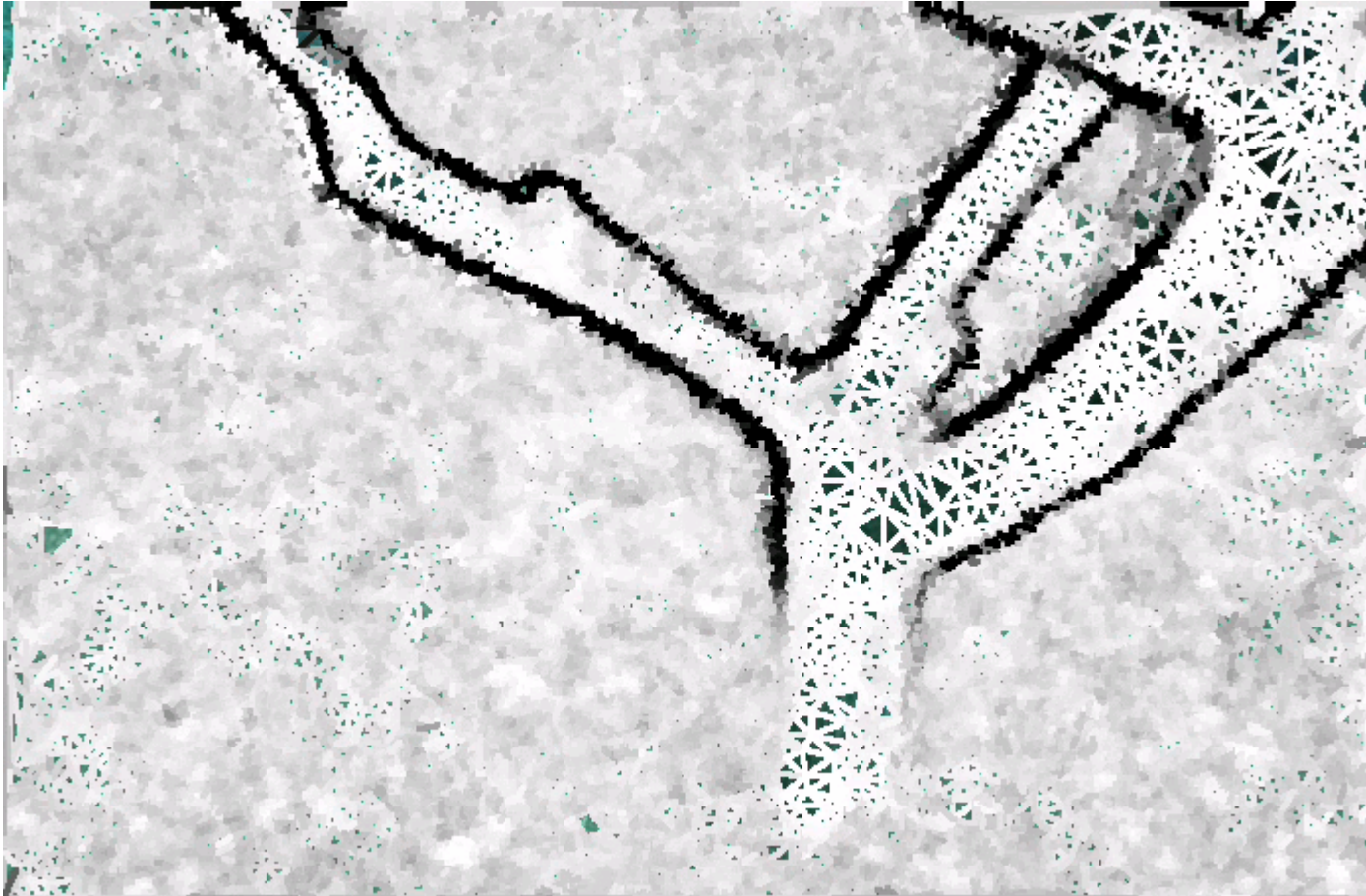


Link Weighting based on Flow Gradient

(lighter = stronger)



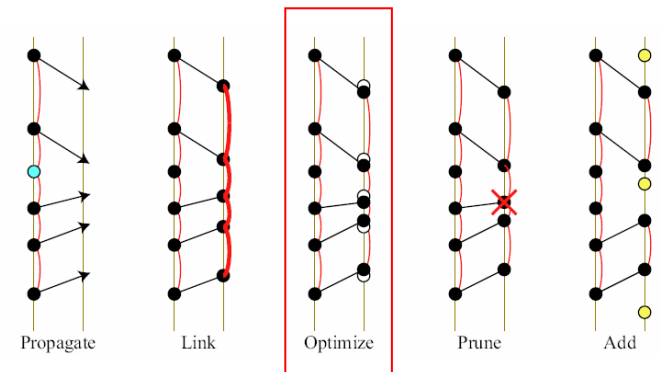
Particle Linking



Particle Optimization

Optimization objective function:

$$E(i, t) = \sum_{k \in K_i(t)} E_{Data}^{[k]}(i, t) + \alpha_d \sum_{j \in L_i(t)} E_{Distort}(i, j, t)$$



Particle Optimization: Data

Data term:

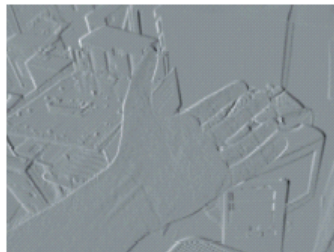
$$E_{Data}^{[k]}(i, t) = \Psi([I^{[k]}(x_i(t), y_i(t), t) - \hat{c}_i^{[k]}(t)]^2)$$



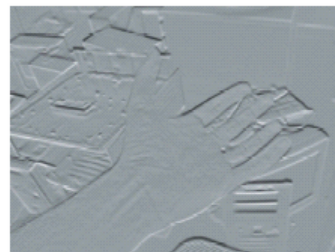
Brightness

Green - Red

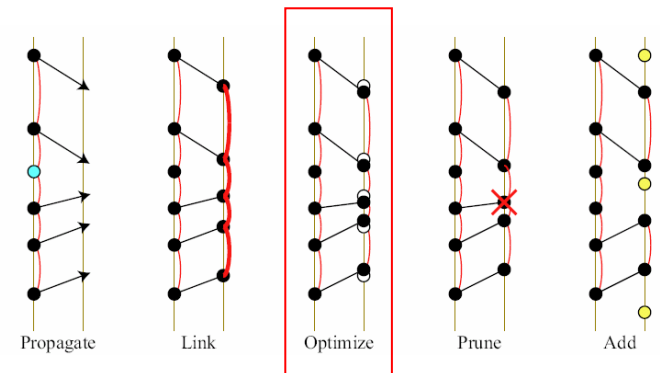
Green - Blue



x Gradient



y Gradient



Particle Optimization: Data

Data term:

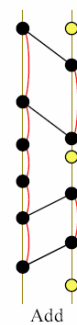
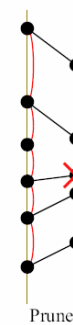
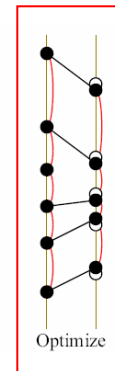
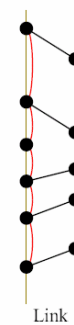
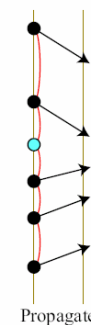
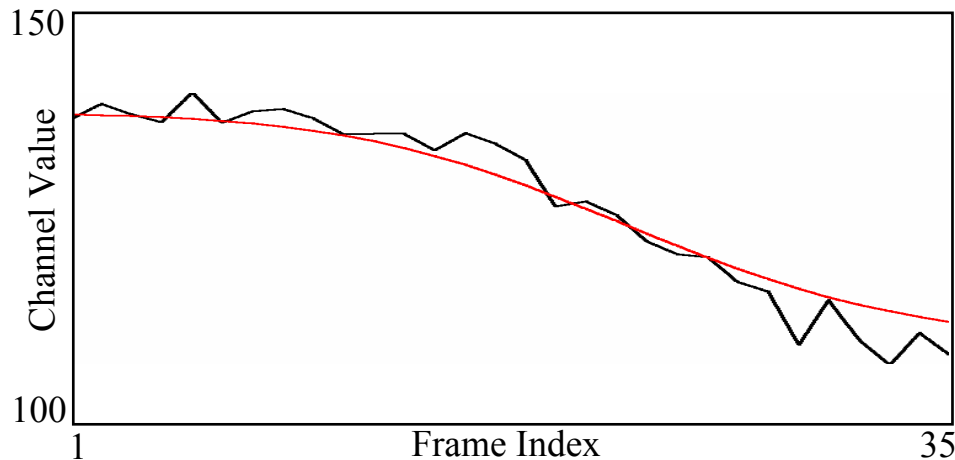
$$E_{Data}^{[k]}(i, t) = \Psi([I^{[k]}(x_i(t), y_i(t), t) - \hat{c}_i^{[k]}(t)]^2)$$



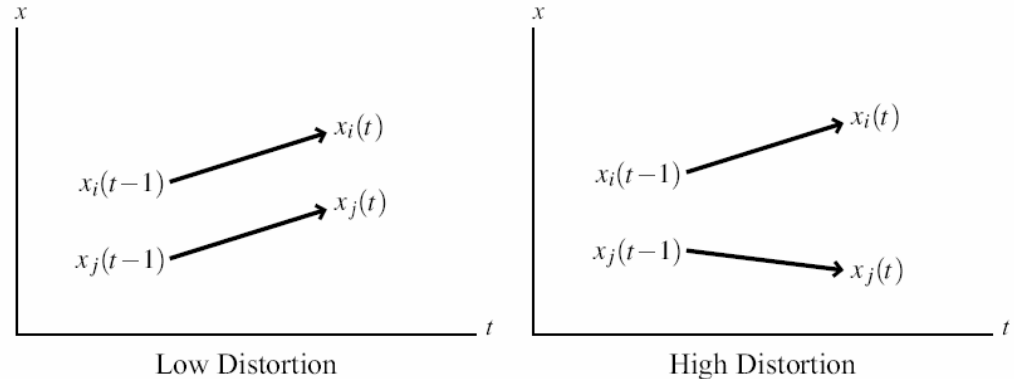
Observed Channel Value



Filtered Channel Value

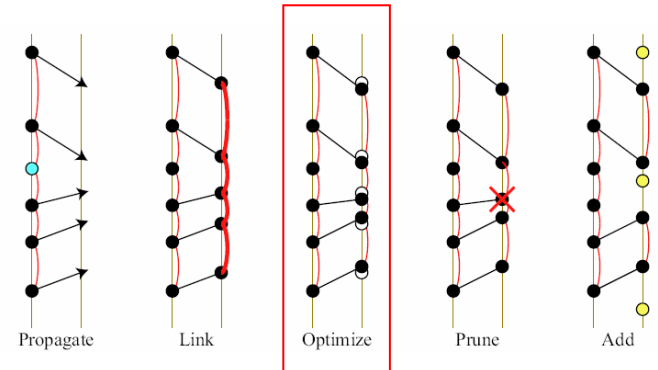
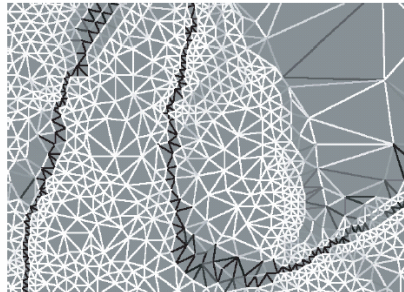


Particle Optimization: Distortion



Distortion term:

$$E_{Distort}(i, j, t) = l_{ij}(t) \Psi([u_i(t) - u_j(t)]^2 + [v_i(t) - v_j(t)]^2)$$



Particle Optimization

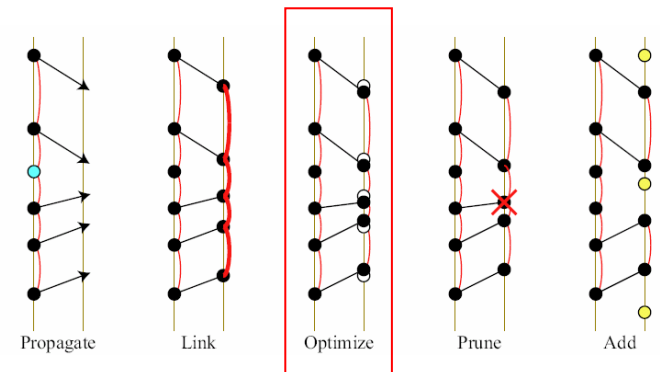
Loop until convergence:

- Solve system for $dx_i(t)$, $dy_i(t)$ using SOR:

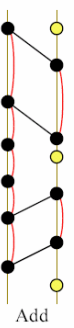
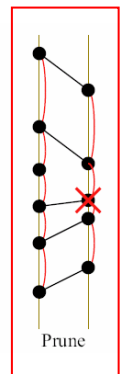
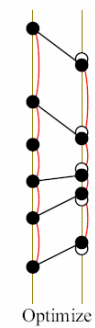
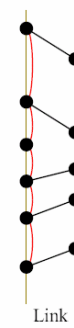
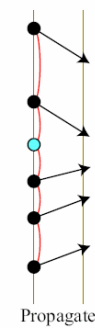
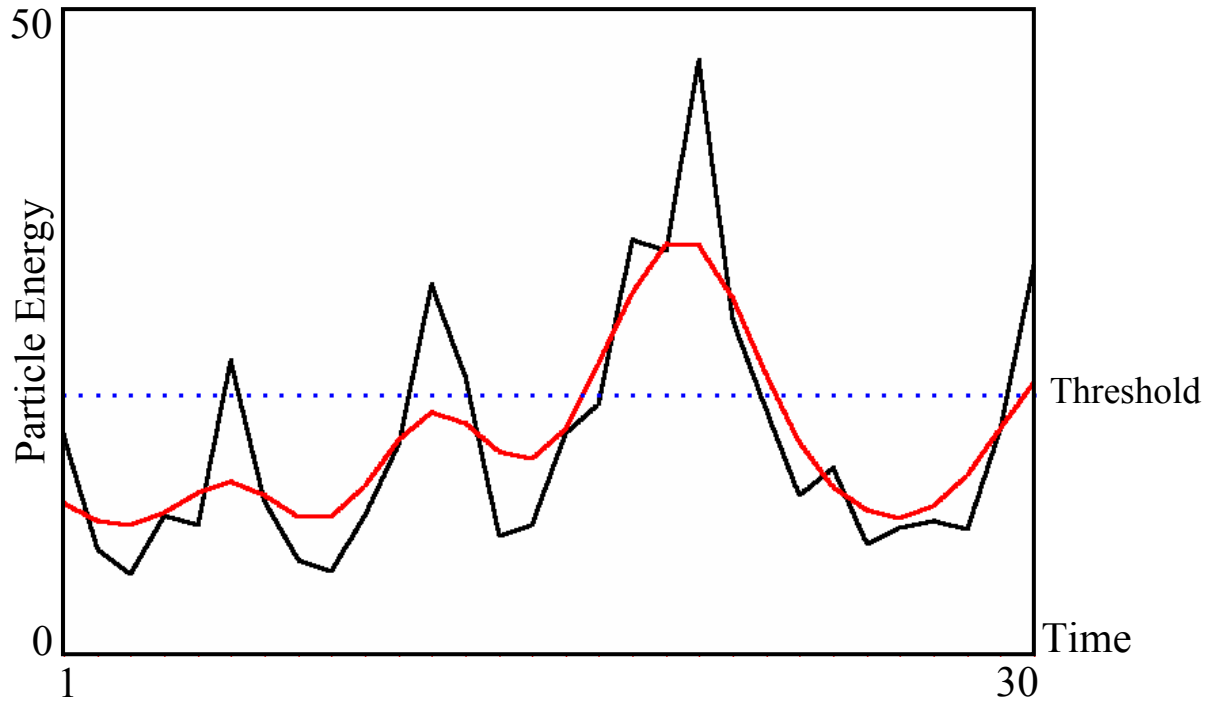
$$\left\{ \frac{\delta E}{\delta dx_i(t)} = 0, \frac{\delta E}{\delta dy_i(t)} = 0 \mid i \in P, t \in F \right\}$$

- $x_i(t) \leftarrow x_i(t) + dx_i(t)$
- $y_i(t) \leftarrow y_i(t) + dy_i(t)$
- Update link weights, etc.

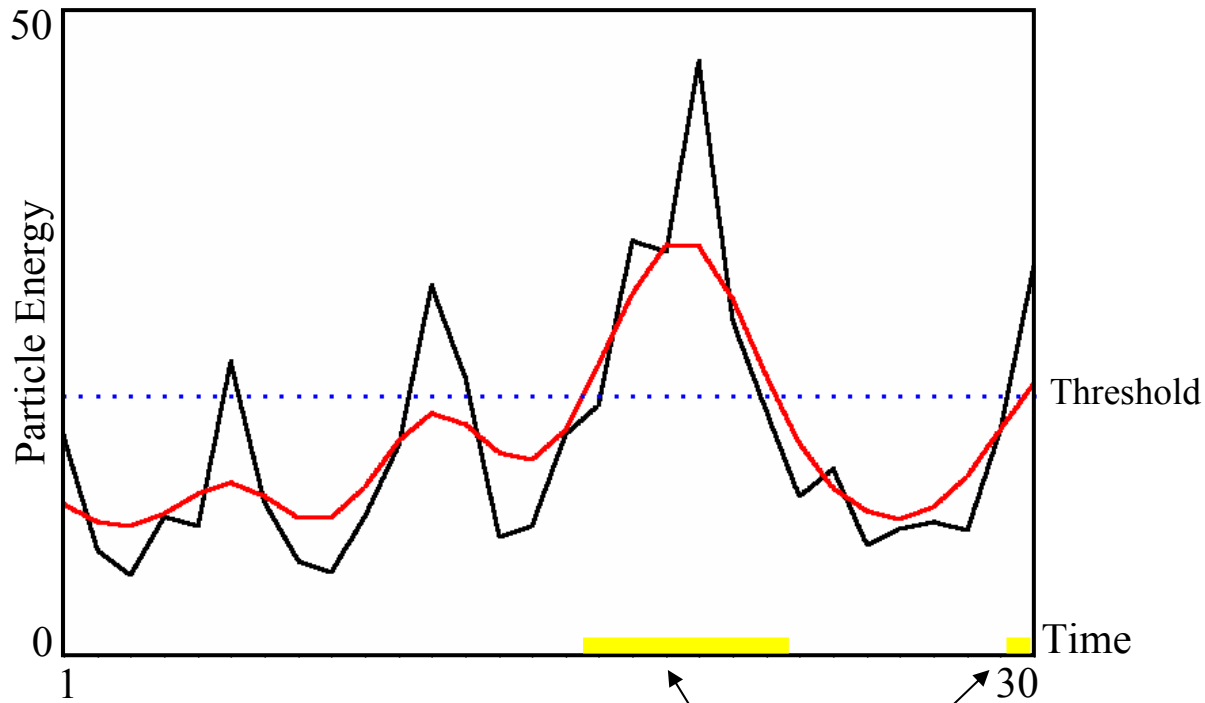
(see paper for more details)



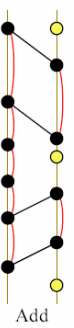
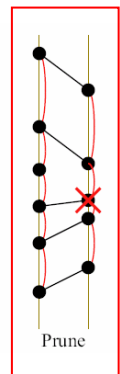
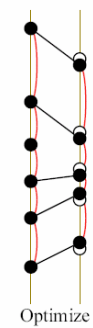
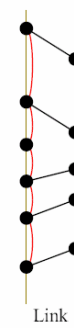
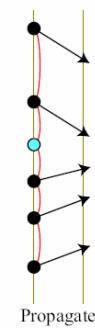
Particle Pruning



Particle Pruning



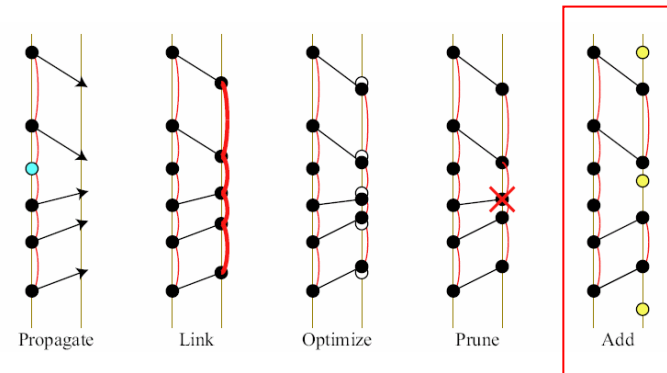
Above Threshold:
Deactivate



Particle Addition



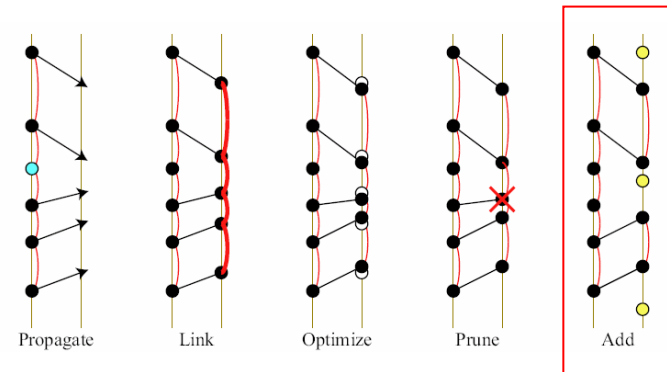
Particle Placement



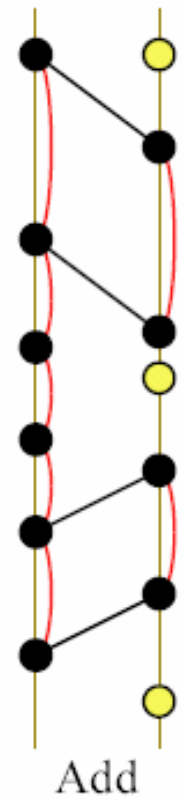
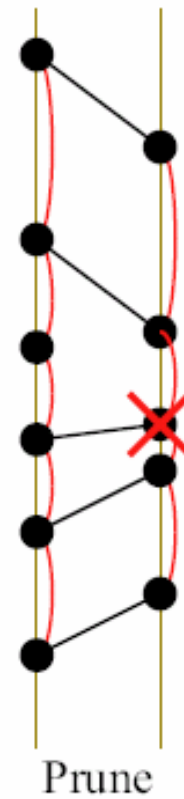
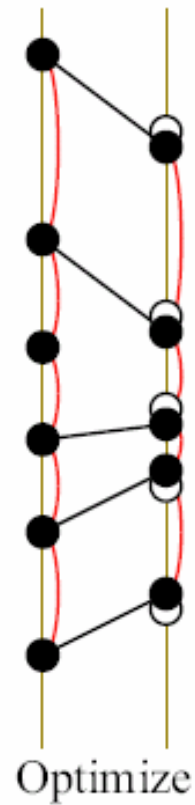
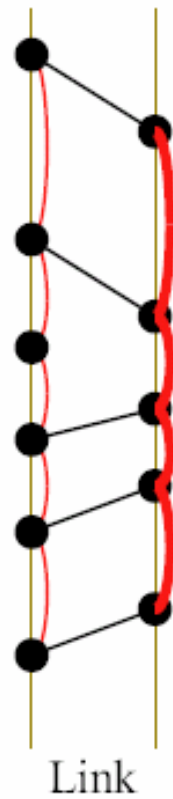
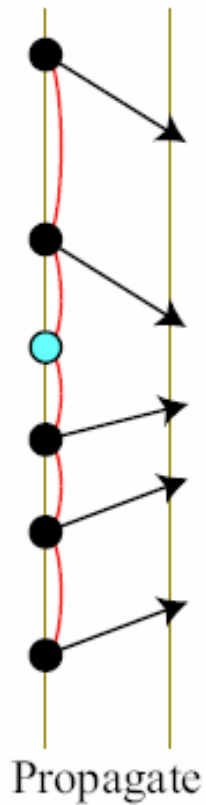
Particle Addition



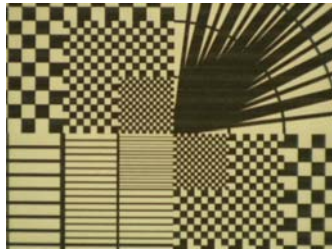
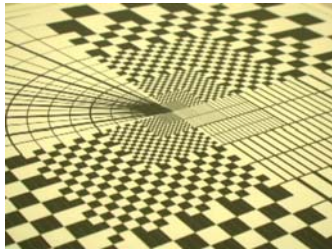
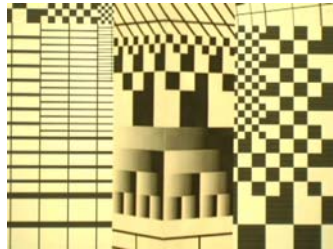
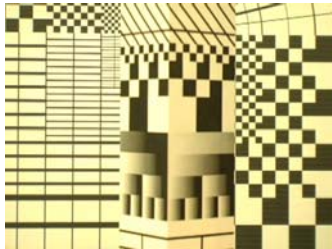
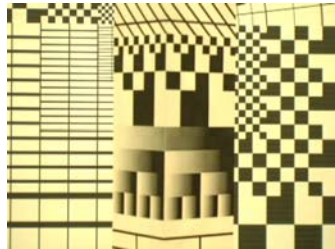
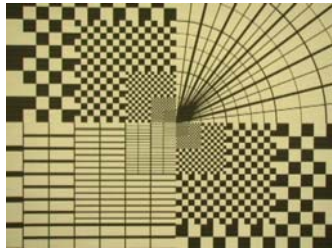
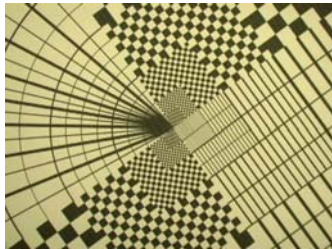
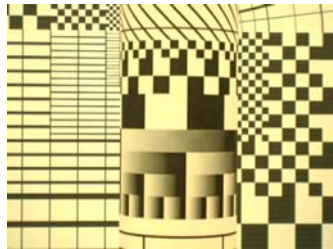
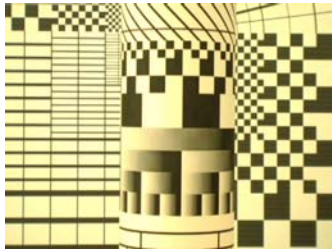
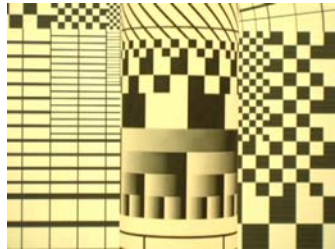
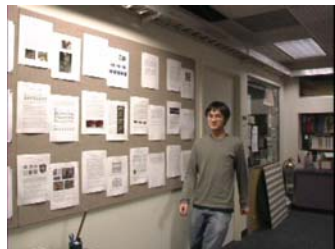
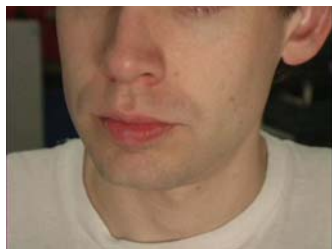
Scale Map



Particle Video Algorithm



Evaluation Videos

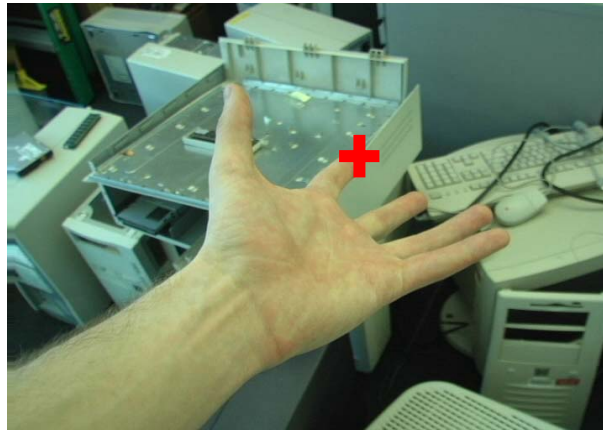


Results / Evaluation

Construct videos that return to the start frame:



1, 2, 3, ...

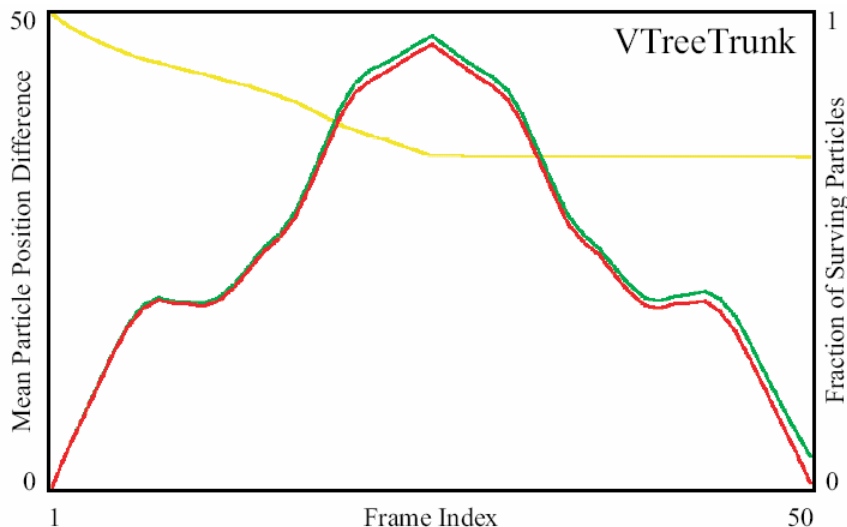
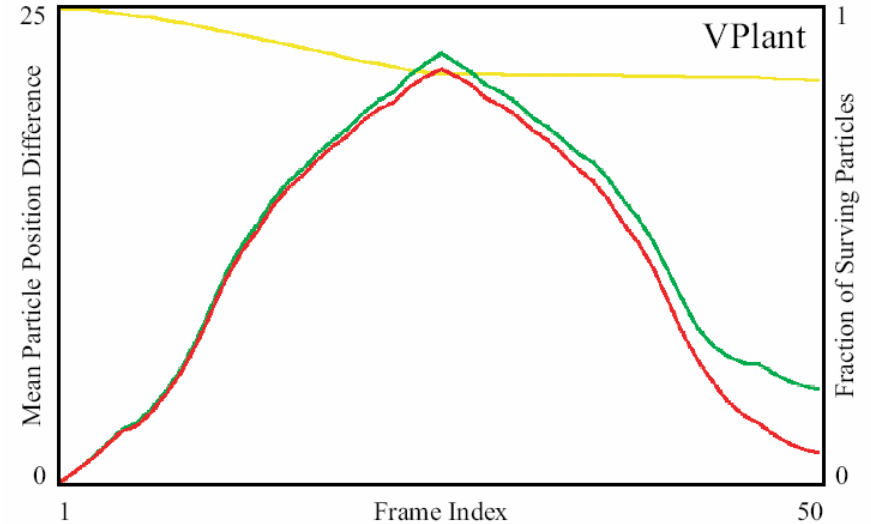
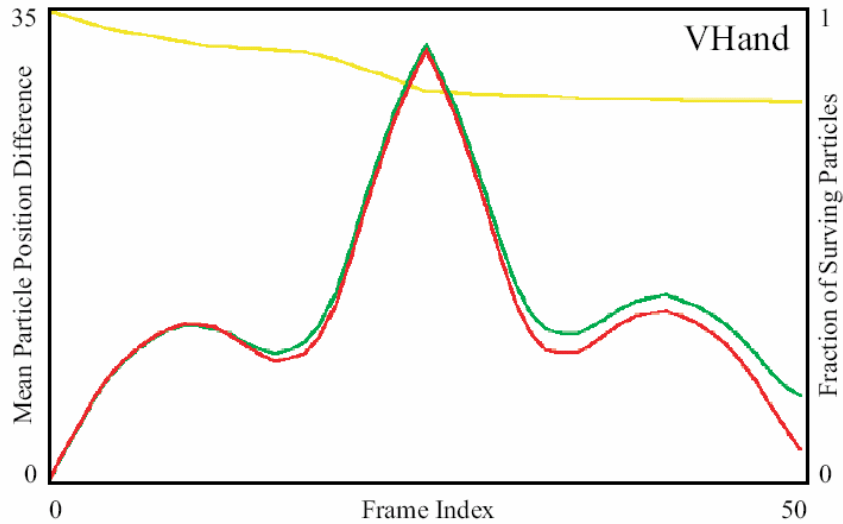


..., N-1, N, N-1, ...



...3, 2, 1

Results / Evaluation



Particle distance: **red**
Concatenated flow distance: **green**
Fraction surviving: **yellow**

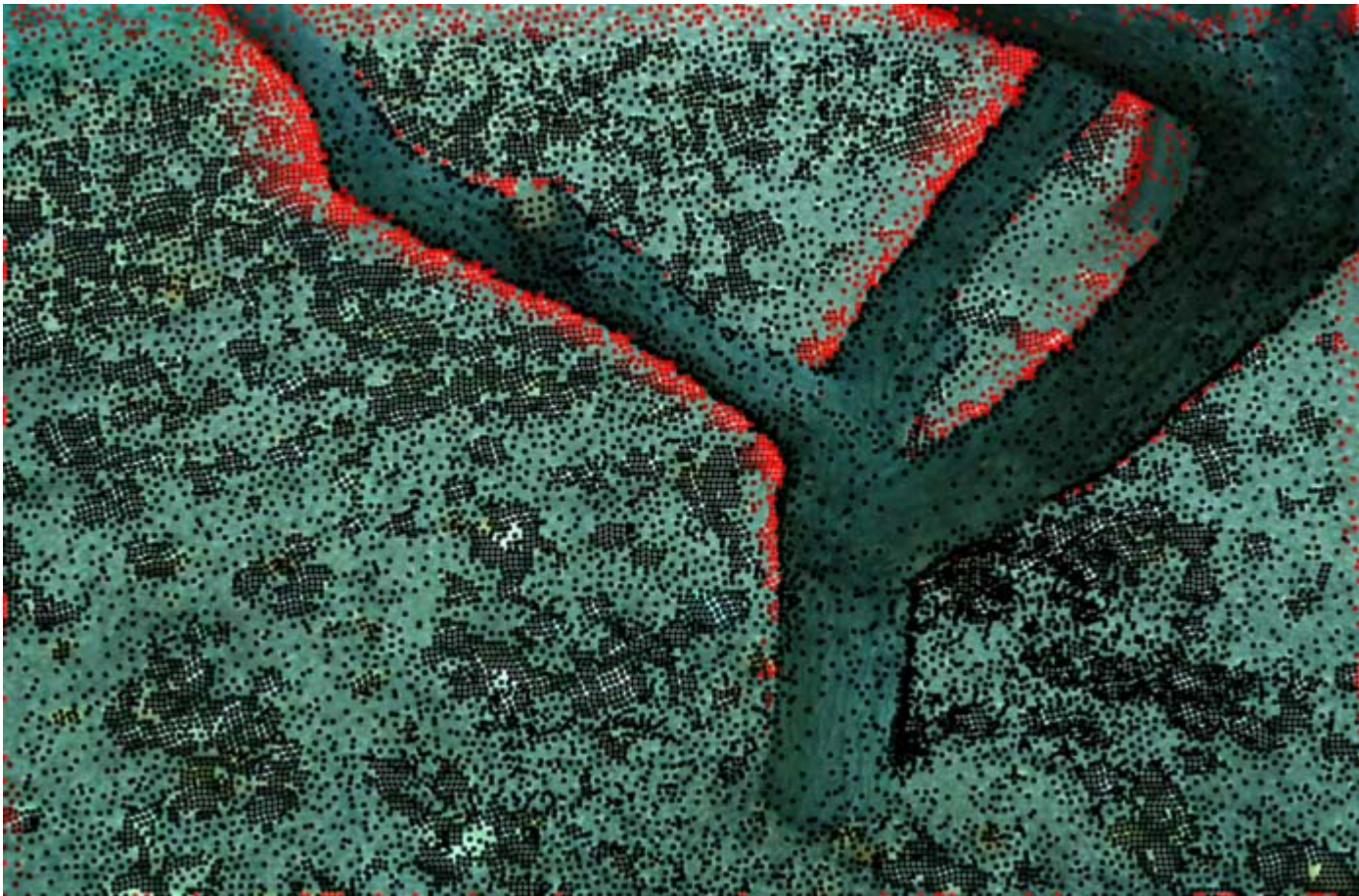
Results / Evaluation



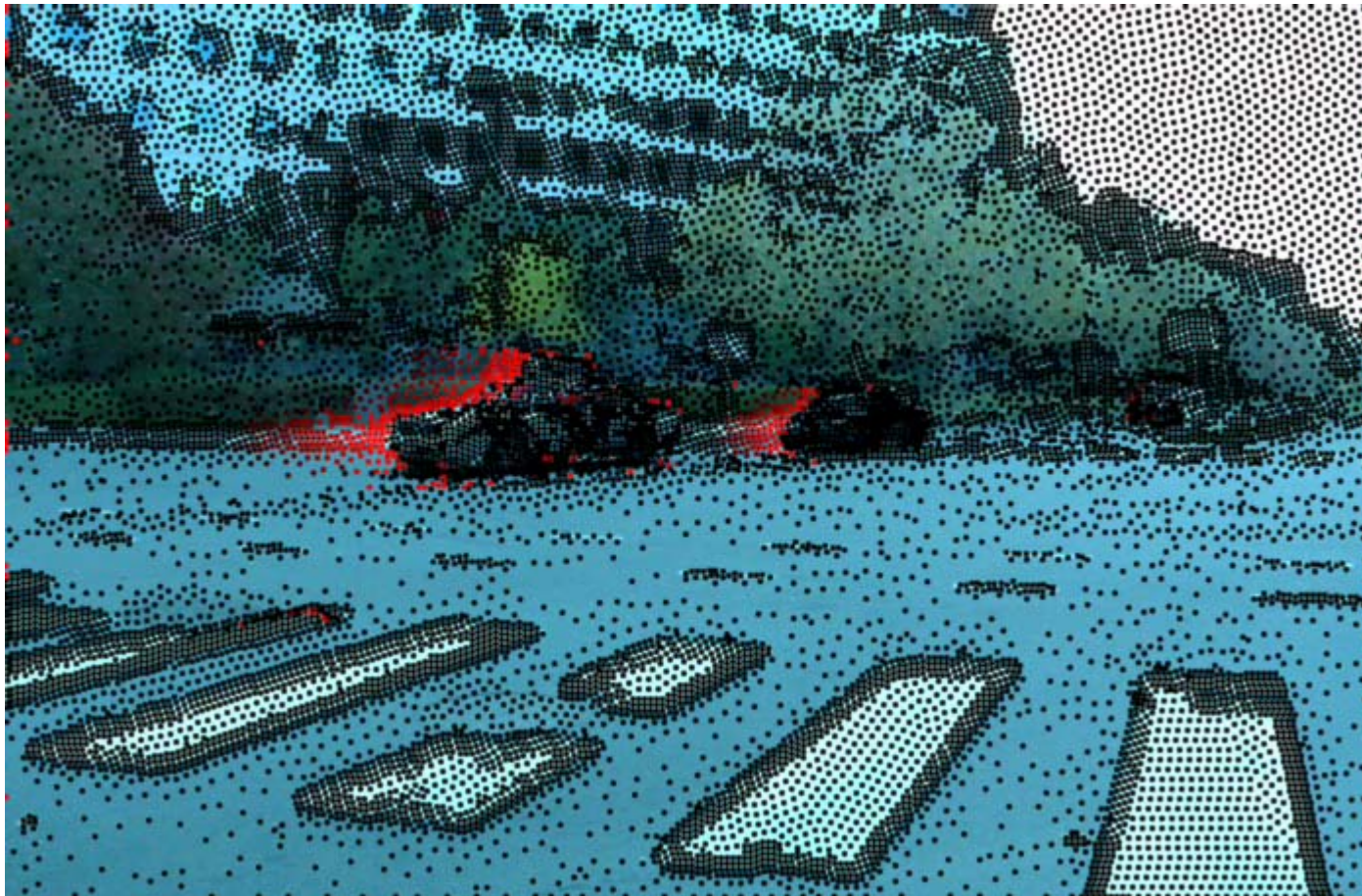
Results / Evaluation



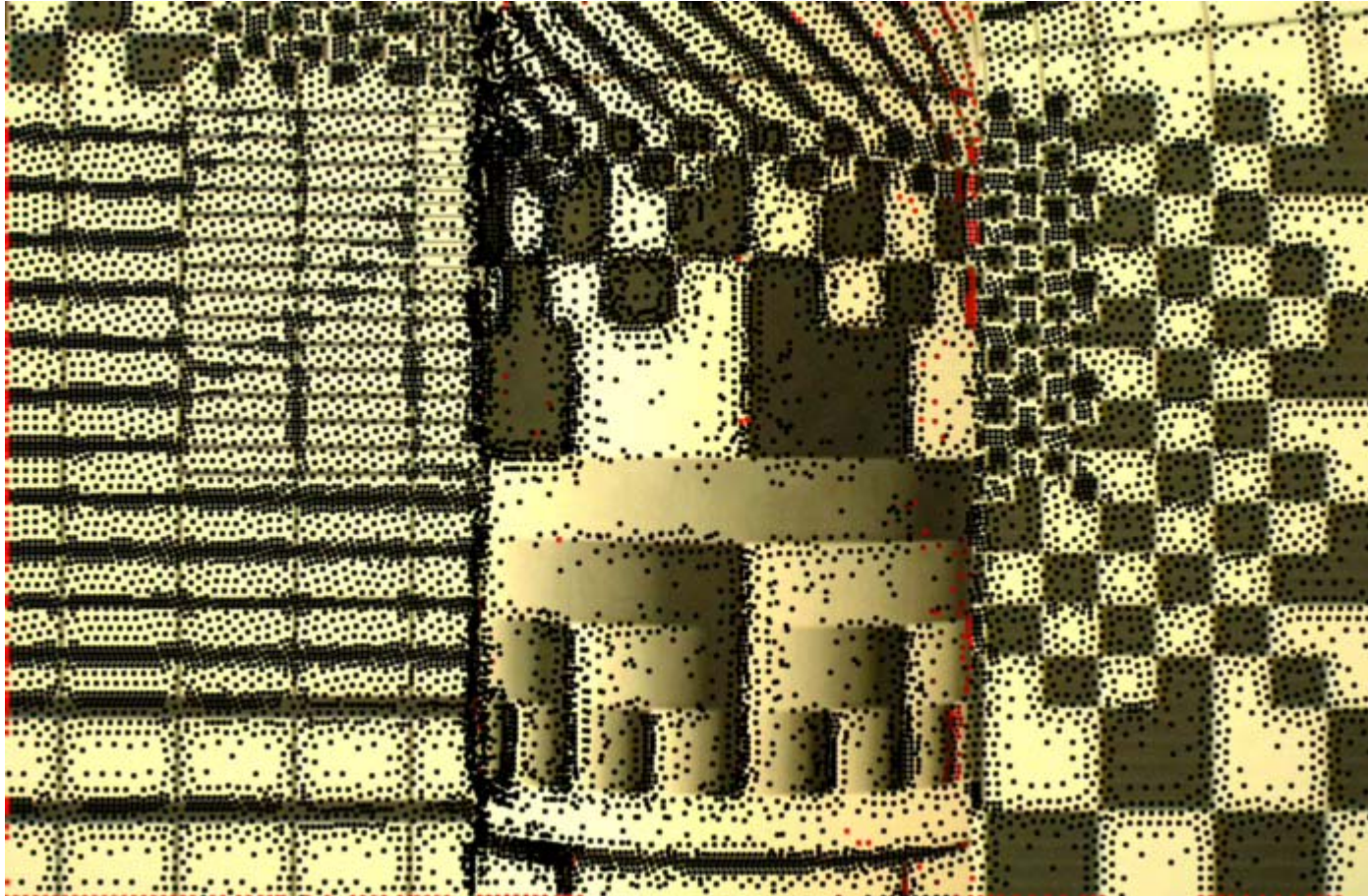
Results / Evaluation



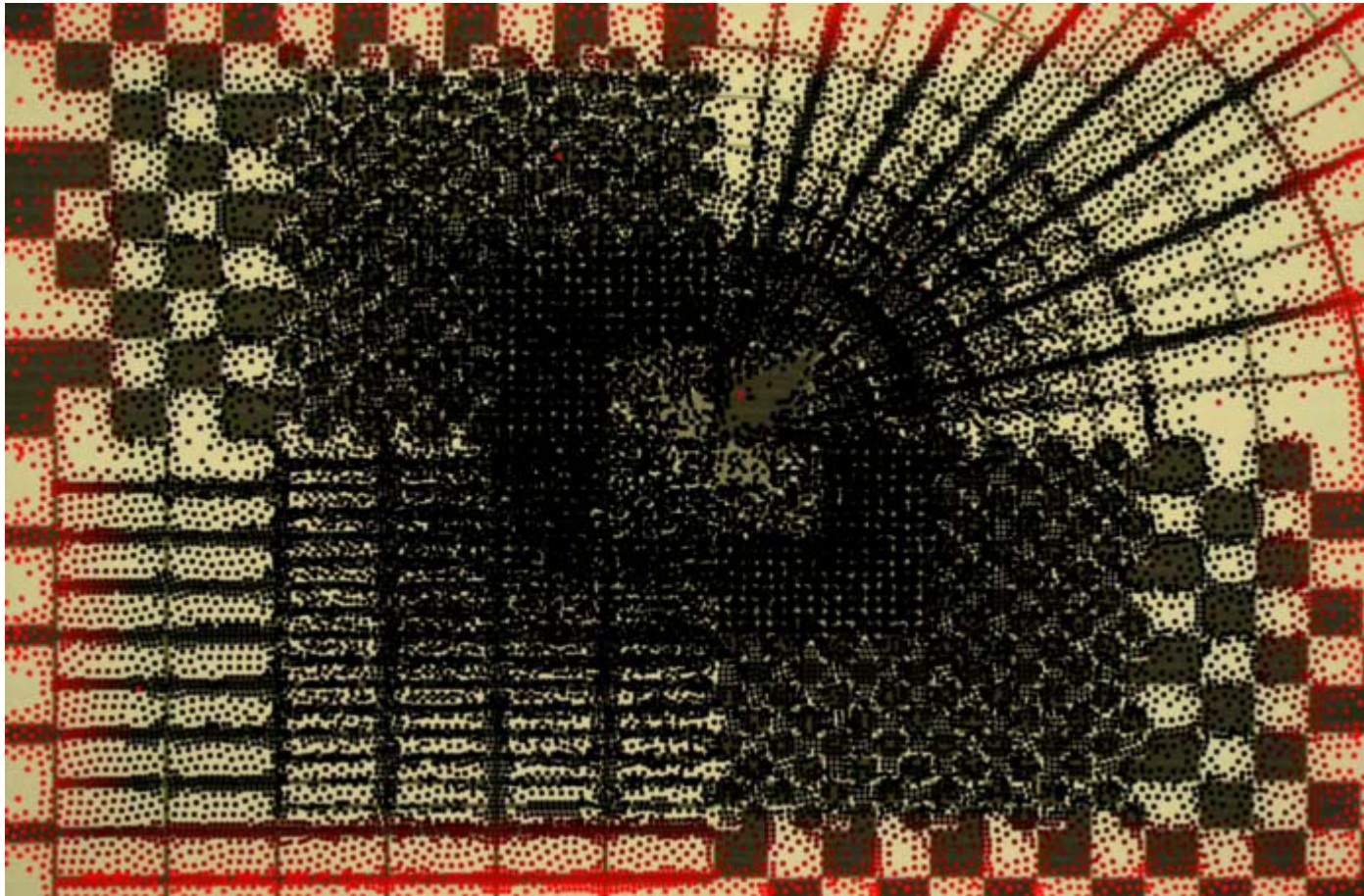
Results / Evaluation



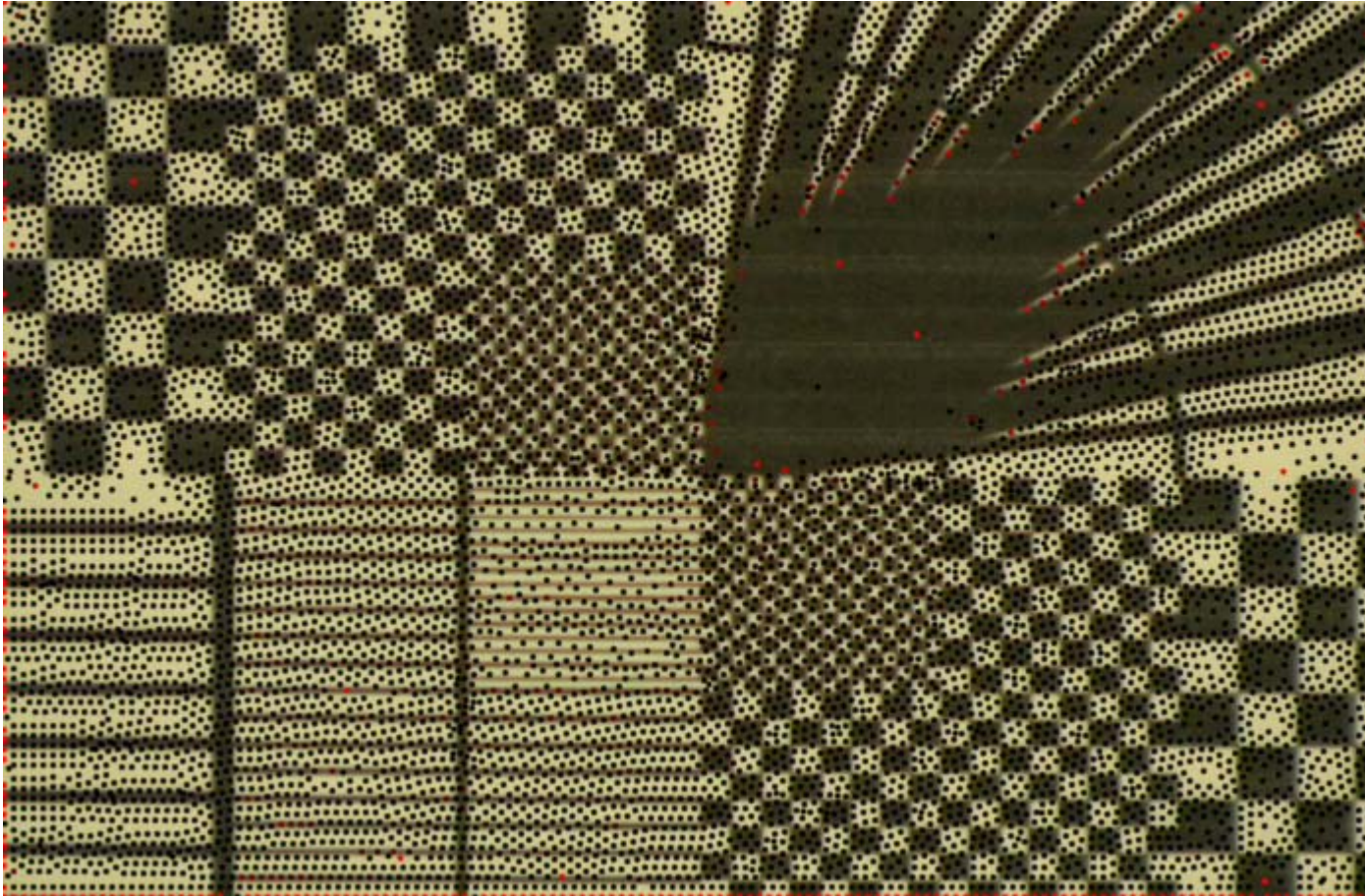
Results / Evaluation



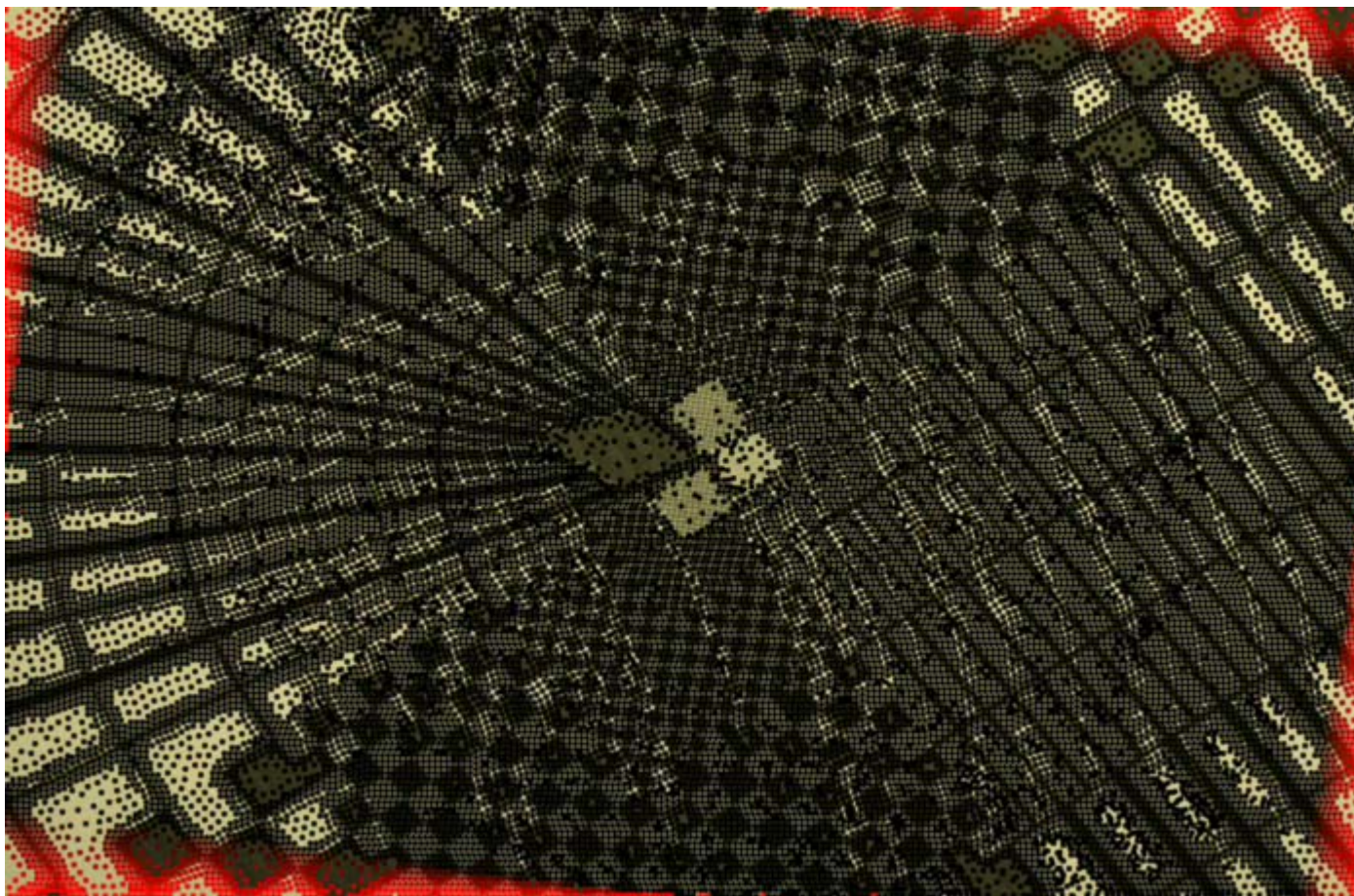
Results / Evaluation



Results / Evaluation



Results / Evaluation



Failure Modes



Failure Modes



Limitations / Future Work

Issue: occlusion handling

Possible solution: analyze local motion histories to distinguish good/bad distortion

Issue: flow dependence

Possible solution: hybrid flow / particle optimization

Limitations / Future Work

Issue: appearance changes due to reflectance and scaling

Possible solution: invariant feature descriptors for particles away from occlusions

Other areas of exploration:

- Faster algorithms (currently 40 seconds/frame)
- Geometric constraints
- Batch particle positioning
- Evaluation on synthetic sequences

Summary

- Particles can represent complex motion and geometry
- Particle representation is useful for application algorithms
- Different from other representations (vector fields, rigid components, layers, tracked feature patches)

More Info

<http://rvsn.csail.mit.edu/pv>

Peter Sand and Seth Teller. *Particle Video: Long-Range Motion Estimation using Point Trajectories*, CVPR 2006.

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